

A Plan to Study the Radiated Emissions from a VASIMR[®] Engine Exhaust Plume

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Abstract: A method to evaluate the radiated electromagnetic interference from a Variable Specific Impulse Magnetoplasma Rocket (VASIMR[®]) propulsion system is presented. Emphasis is placed on the interference produced or transmitted through the exhaust plume of the rocket. The method involves experimental measurements within the plasma plume, receiving antenna measurements in the vacuum chamber, analytical modeling of plasma instabilities, and simulation. The primary goal of the study will be to assess the compliance of a VASIMR[®] engine with the electromagnetic compatibility requirements of the International Space Station and other spacecraft standards. More generally, the study will explore the subject of instabilities in a plasma jet expanding through a magnetic nozzle.

Nomenclature

f_{ci}, f_{ce}	= ion, electron cyclotron frequencies	n_e	= electron number density
f_{pi}, f_{pe}	= ion, electron plasma frequencies	$\Delta n/n$	= plasma density fluctuation
f_{LH}, f_{UH}	= lower hybrid, upper hybrid frequencies	ω	= angular frequency
$f(v)$	= velocity distribution function	x	= position along ray path
r	= radius in cylindrical chamber coordinates	D	= dispersion relation
z	= axial chamber coordinate	k	= wave vector
E	= electric field vector	Γ	= wave growth rate
B	= magnetic field vector	ρ	= gyroradius
σ	= conductivity tensor		

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I. Introduction

The Aurora mission will consist of the Variable Specific Impulse Magnetoplasma Rocket (VASIMR®) VF-200™ operating as an attached payload on the International Space Station (ISS). The rocket must meet certain limits of radiated electromagnetic interference (EMI). In this paper, we outline a plan to study the EMI from the exhaust plume of the VASIMR® VX-200 prototype within its 150 m³ vacuum facility at the Ad Astra Rocket Company (AARC) located in Webster, TX. The study will include probe measurements within the plasma plume, receiving antenna measurements in the vacuum chamber, analytical modeling of plasma instabilities and wave propagation, and simulation. The paper is organized as follows: In the remainder of the introduction, we discuss the radiated EMI compatibility requirements for ISS payloads and accepted EMI testing methods, followed by an overview of the VASIMR® VX-200 laboratory prototype and the planned VF-200™ space propulsion system. In Section II, we present methods to measure and model the EMI from the VX-200 engine, with subsections devoted to: radio frequency waves injected from the couplers in the rocket core, macroscopic and microscopic instability growth rates, nonlinear wave amplitude limits, simulating wave propagation, particle simulations, and receiving antenna measurements.

A. Laboratory Setup & VASIMR® Basics

A VASIMR® engine is a two-stage RF driven magnetized plasma rocket. The first stage (helicon) is a helicon plasma source. The second stage (ICH) heats the ions using left hand polarized slow mode waves launched from the high field side of the ion cyclotron resonance.¹ Two major elements of a VASIMR® engine are the RF power processing systems and the high magnetic field enabled by state-of-the-art superconducting magnet technology. The unique element of the VASIMR® technology resides in the bore of the magnet and is referred to as the rocket core. This is where the electromagnetics and structure of the system are carefully designed to couple RF power to the dense magnetized plasma.

Figure 1 shows a conceptual schematic of a single VASIMR® thruster. A VF-200™ engine is a specific embodiment of two such thrusters with opposing magnetic polarity clustered such that they form a magnetic quadrupole. This nulls any torque in earth's magnetic field and greatly reduces any stray magnetic field strength around the spacecraft. The VF-200™ is the flight design which will be operated as an attached payload on the ISS. In the meantime, EMI testing will begin

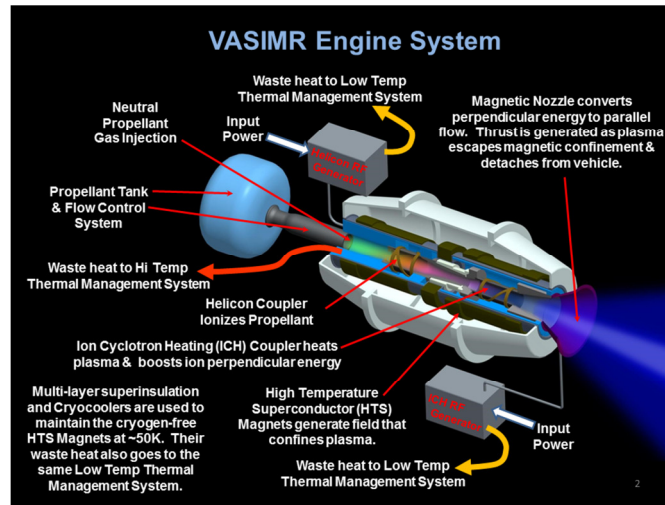


Figure 1. Schematic diagram of a VASIMR® System

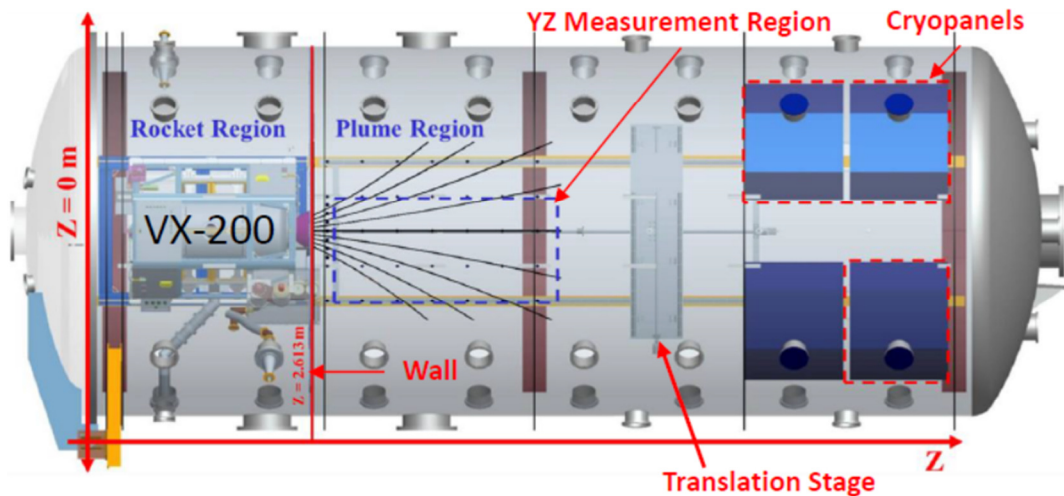


Figure 2. Schematic of the 10 m long x 4.3 m diameter vacuum chamber and the VX-200™ engine

using the VX-200 laboratory device, which has been operated since 2009 in support of the VF-200™ design process. The remainder of this section discusses the VX-200 and its laboratory configuration.

The VX-200 device is a 200 kW laboratory prototype that has been operated at specific impulses between 2000 s and 5000 s, and thrusts up to 6 N. The magnetic field is generated by a cryogen-free, generation 1 (Nb-Ti) superconducting magnet encased in a well-insulated cryostat surrounding the engine core. The magnet produces a peak magnetic field strength of 2 T. The RF power is generated from two high-efficiency solid-state generators manufactured by Nautel Limited of Canada. Impedance matching circuits are used in the transmission lines from the RF generators to the couplers in the rocket core. Argon propellant is regulated through an injector plate into the first stage using a Moog propellant manifold.

The VX-200 is operated in a stainless steel vacuum chamber (see Figure 2) that is 4.3 m in diameter and 10 m long with a volume of 150 m³ (including the end caps) located at the AARC facility. The chamber is partitioned into two regions: a rocket region (upstream) and a plume region (downstream). The two regions were previously separated by an aluminum framed wall with Lexan paneling, but this partition is presently being upgraded to a stainless steel wall. The majority of the VX-200 components are located within the vacuum chamber, but the RF generators, magnet power supplies, and magnet cryocoolers are operated outside in atmospheric pressure.

B. Radiated EMI Compatibility Requirements

ISS payloads are subject to limits on narrowband radiated emissions from 14 kHz to 20 GHz.² More generally, space propulsion systems are tested for radiated EMI in accordance with MIL-STD-461.³ Procedures for testing EMI require measuring the radiated electric field at a distance of one meter from the equipment under test.⁴ Ion engines and Hall thrusters have typically been tested in electromagnetically anechoic rooms specially designed for measuring the EMI of electric propulsion (EP) devices.^{5,6} In some cases, the thruster is mounted inside of a dielectric (e.g. fiberglass) tank while the exhaust flows into a larger plenum. A receiving antenna is mounted outside of the dielectric tank, within a larger, anechoic room that is designed to shield the antenna from external noise and minimize reverberation within the enclosure.⁶

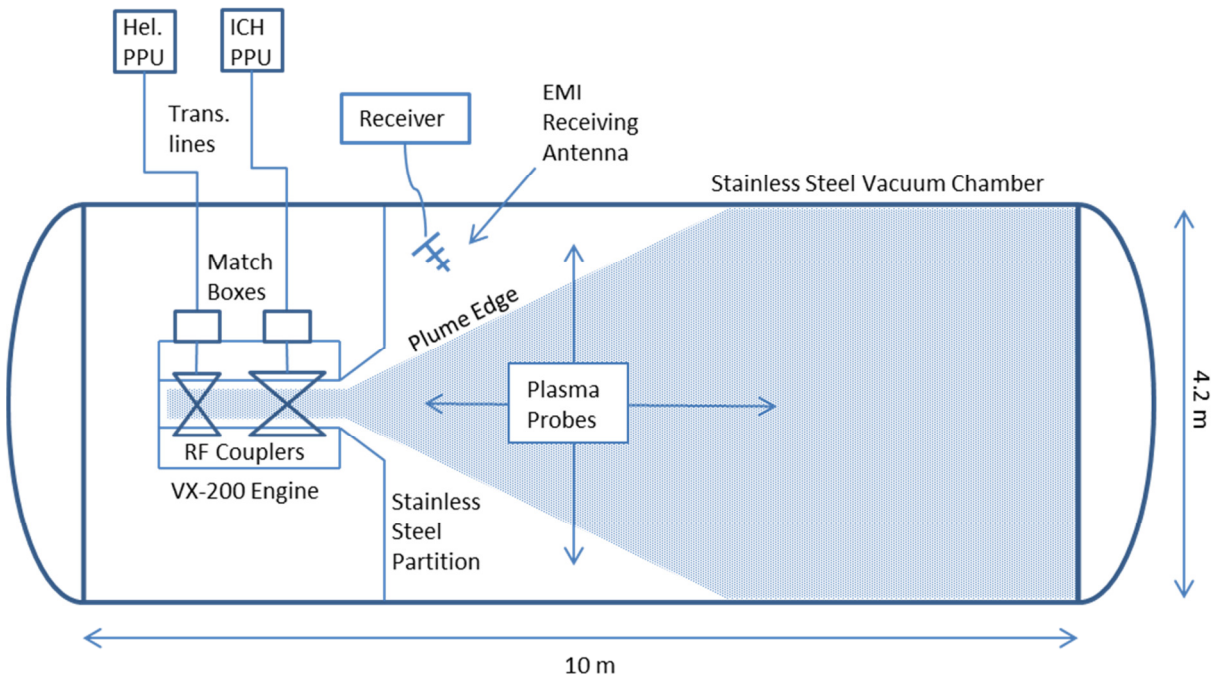


Figure 3. Conceptual Schematic of Receiving Antenna Placement for Plume EMI Study. Possible sources of EMI include: RF PPUs, matching networks, transmission lines, rocket core, and the plasma plume. This paper focuses on measuring and modeling EMI from the plume.

This paper is intended to be a first step in addressing the challenges associated with measuring the EMI from the plume of a 200 kW VASIMR® engine. The possible sources of radiated emissions from a VASIMR® device can be broadly grouped into three categories: emissions from the radio-frequency (RF) power generators, transmission lines, and matching networks; emissions from the first and second stage couplers, radiated directly or through the

plasma; and emissions generated from plasma instabilities in the exhaust plume of the rocket. The strategy for measuring the EMI from each of these sources is as follows.

The VX-200 RF generators currently operate outside of the vacuum chamber. They will be tested for EMI in the laboratory in accordance with the “open field site” provision of the EMI testing requirements⁴, although the flight generators will eventually need to be tested as part of the complete VF-200™ engine assembly. The first and second stage couplers are integral to the VX-200 rocket core, which must be tested inside the vacuum chamber. The chamber in this case will serve as an RF enclosure. Receiving antennas will be placed within the upstream section of the vacuum chamber to measure the EMI propagating radially outward or upstream from the rocket core.

A typical EMI study of an EP device would involve only the testing in the preceding paragraph. In addition to these tests we intend to study waves that are transmitted through the exhaust plume, being directly propagated from the couplers or generated by instabilities in the plume. Receiving antenna measurements will be made in the downstream section of the vacuum chamber, treating the plasma as a transmitter. The remainder of this paper will discuss only the EMI from the plasma plume. Figure 3 shows the general plume EMI testing arrangement in the chamber, along with the other potential sources of EMI. In previous studies, the plume-vacuum boundary has been defined as the

The AARC vacuum facility may need to be modified to meet the requirements for EMI testing.⁴ To limit reverberation during receiving antenna measurements, we may have to temporarily install electromagnetic absorbent material on the interior walls of the vacuum chamber. Since the AARC chamber is large enough to study the expansion of the plasma plume into vacuum⁷, we expect that much of the relevant plasma wave dynamics will be present in this laboratory study. Even if the chamber could be made perfectly anechoic, however, the waves propagating through the plasma plume could still be affected by the presence of the conducting walls. For this reason, we will use theoretical estimates and numerical simulation, in addition to the traditional antenna measurements, to study the electromagnetic emissions from the plume.

II. Plume EMI Study Plan

Our challenge is to use measurements, taken in and around the plasma plume region inside the vacuum chamber, to predict radiated wave properties for the boundary conditions that would be expected in a space environment. We outline a logical, question based process for this study in Figure 4.

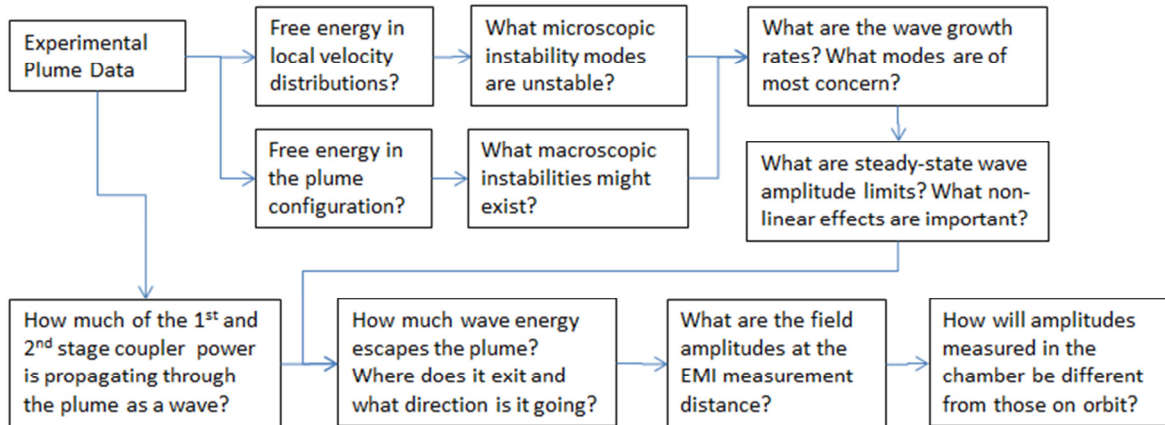


Figure 4. Logical Process for Relating Probe Measurements to Emissions

A. Previous Studies of Plume Oscillations

The primary tools for searching for waves within the plume will be probe measurements of $\mathbf{E}(\omega)$, $\mathbf{B}(\omega)$, and density fluctuation ($\Delta n/n(\omega)$). Preliminary studies of the electric fields in the plume region have already been reported.^{7,8} Olsen et al measured radial electric field oscillations at frequencies approximately three times the lower hybrid ($\sim 3f_{LH}$) along the plume edge. The oscillations were prominent up to a certain axial distance and then quickly disappear. It was also clear that the oscillations were confined to the plume. (The plume edge in these studies was based on measurements of axial ion flux.) The radial electric field oscillations are suspected to be related to the plasma detachment process, and they will be one of the first subjects of the instability modeling effort. An extension

of these probe measurements is planned, wherein the axial and radial components of the electric and magnetic fields will be measured across the frequency spectrum of concern for EMI.

B. Propagation of the Coupler Drive Frequencies

The VX-200 coupler drive frequencies will be the first subjects of our EMI testing, since they are an intentionally generated source of electromagnetic energy. The first stage of the rocket core uses a commercial standard frequency in the FM band, while the second stage drive frequency is in the AM band. AARC routinely employs a full-wave simulation method to model the propagation and absorption of the input RF energy into the plasma within the rocket core. As a first step in the EMI modeling process, we will extend the domain of the full-wave simulation further into the plume, providing a first approximation of the injected RF amplitudes within the plume. These amplitudes will be compared to measurements of the vector electric and magnetic fields within the plume. Depending on the results of this comparison, we may have to modify the full-wave code to more closely model the plasma in the plume.

C. Modeling the Plasma Exhaust Plume as a Source of EMI

Figure 5 shows the natural frequencies in the probe measurement region inside the plasma plume. The frequencies in this region span at least six orders of magnitude, all of which lie within the range of concern for EMI compatibility. The plasma transitions from a high field in the rocket core, through several orders of magnitude in field strength, to unmagnetized ballistic trajectories downstream.^{7,8} These transitions complicate the choice for modeling assumptions, and make it difficult to simulate long sections of the plume flow with one numerical algorithm.

One can also infer that, as the magnetic field strength and plasma density decrease as one looks downstream of the probe measurement region, the natural oscillations will occur at lower frequencies. We hope to conservatively estimate the emissions from the full extent of the laboratory plume, including the regions that are inaccessible to both plasma probes and receivers mounted outside the plume.

There are two major classes of instability: macroscopic instabilities that are driven by the free energy of an unstable configuration and microscopic instabilities that tap the free energy of non-equilibrium distribution functions. The former will be investigated addressed by a combination of analytic energy principle estimates and two-fluid simulations. Addressing the latter will require a method that uses plasma probe data as input. The microinstabilities generally occur at frequencies greater than the ion cyclotron and can range over all natural frequencies of the plasma, while macroinstabilities generally occur at lower frequencies.⁹

A review of the relevant literature indicates that instability modeling is nearly always motivated by the direct observation of specific instabilities or by some experimental evidence of their existence. Many instability phenomena are, in fact, named for the way in which they become manifest in experimental data, e.g. “flute” instability, “sausage” instability, “fire hose” instability. Similarly, we are concerned with that contribute to EMI observations. Our aim is to perform an investigation over a broad frequency range to determine what modes, if any, cause significant EMI into the

vacuum region surrounding the plume. This instability investigation will help guide direct measurements of EMI in the vacuum chamber. The investigation will also help to determine what emissions measured in the vacuum chamber will be important for meeting electromagnetic compatibility requirements. There are too many possible modes, however, to model them all simultaneously and accurately. Our modeling efforts must therefore be guided by experimental observations of instability, by emissions in the vacuum, or by theoretical arguments as to what

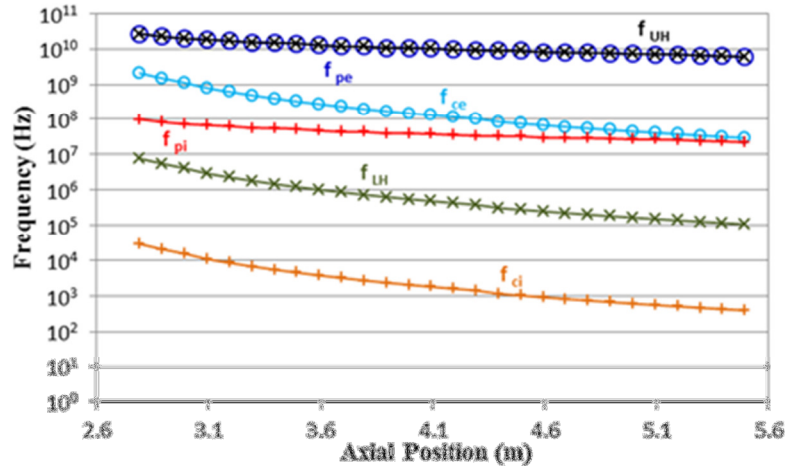


Figure 5. Natural frequencies along the plume axis in the probe measurement region: f_{ci} (ion cyclotron), f_{LH} (lower hybrid), f_{pi} (ion plasma), f_{ce} (electron cyclotron), f_{pe} (electron plasma), f_{UH} (upper hybrid)

instabilities might exist in the plume, given the observed configuration. In Figure 6, we outline the practical method by which we will investigate the possible instabilities in the plasma plume.

D. Macroscopic Instabilities

Our investigation of macroscopic instabilities will begin with analytical calculations of growth rates using published formulae. We will use experimental data to model the plume configuration.

Two fluid simulations will be performed based on the results of analytical investigation. We anticipate that the treatment of ions and electrons as separate fluids will be required, especially in downstream sections of the plume where the electrons remain magnetized but the ions are beginning to detach from the magnetic nozzle. Additionally, it is only the ions that are heated in the second stage of the VASIMR[®] engine core, which further motivates the separate treatment of the ions and electrons.

A VASIMR[®] engine exhaust was previously simulated using the NIMROD code with the goal of studying the plasma detachment process.¹⁰ The NIMROD code was designed to study long-wavelength, low-frequency, nonlinear phenomena in toroidal plasmas.¹¹ The previously reported study was only preliminary, treating the ions and electrons as a single fluid and using a generalized Ohm's Law and the adiabatic equation of state. The results were somewhat inconsistent with experimental observations. The code does have a provision for treating the electrons as a separate fluid with an electron temperature¹⁰.

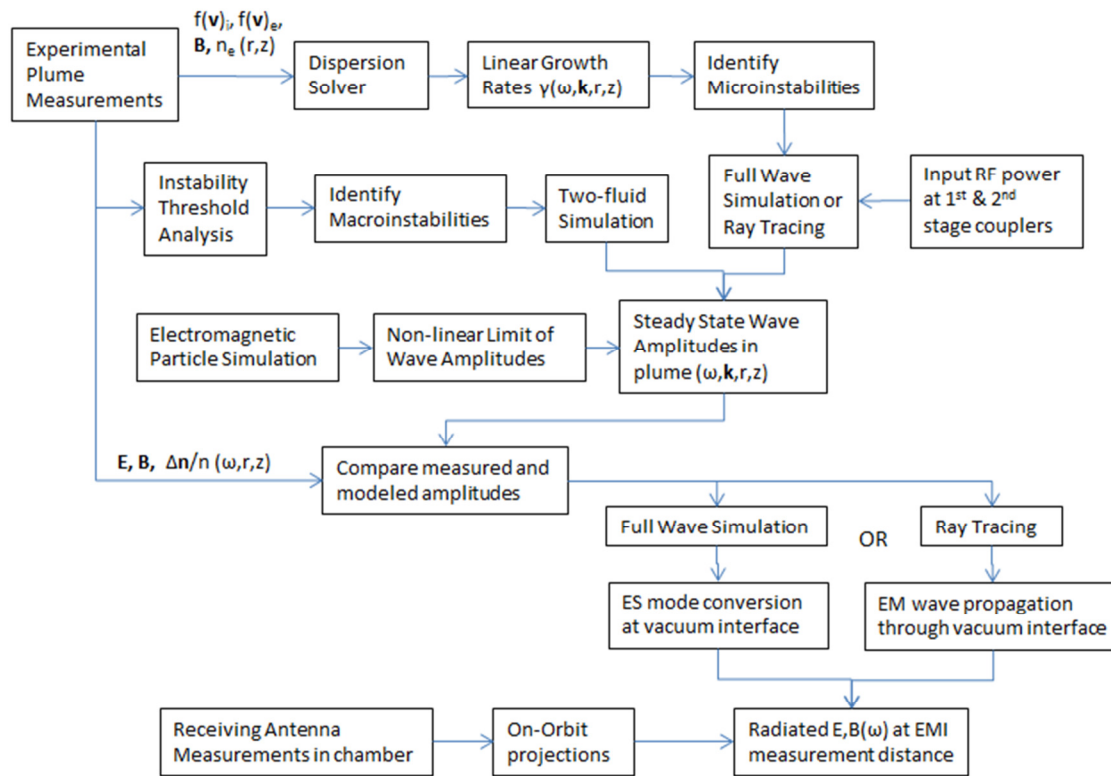


Figure 6. General Plume EMI Study Methodology

E. Microscopic Instabilities: Dispersion Analysis

We will determine the availability and distribution of free energy in the plasma by measuring the ion and electron velocity space distribution functions, and the cold plasma density and temperature, on a 2-d grid spanning the exhaust chamber equatorial plane. The velocity distributions will be measured by retarding potential analyzers, ideally with articulating heads, so that the pitch angle distribution can also be measured. The velocity distribution, along with the plasma density and the cold plasma temperature, will serve as input to a numerical dispersion solving algorithm. This method will produce growth rates for all 3 normal modes as a function of frequency.

One attractive numerical algorithm is that of Matsuda and Smith.¹² The method solves the dispersion relation (Eq.) for a uniform, infinite plasma in a uniform magnetic field, $\mathbf{B}_0 = B_0 \hat{z}$. The code allows for input of an arbitrary

velocity distribution, given by values on a two-dimensional velocity space grid, or by analytic functions. This method would preclude without the need to fit the RPA data to a sum of model distributions.¹² We would execute this algorithm at each point in our 2D experimental measurement grid, thereby creating a map of growth rate vs. wave number for an arbitrary propagation angle at each point in the plume.

$$\left| \left(1 - \frac{c^2 k^2}{\omega^2} \right) \mathbf{I} + \frac{c^2}{\omega^2} \mathbf{k} \mathbf{k} + \frac{4\pi i}{\omega} \boldsymbol{\sigma} \right| = 0 \quad (1)$$

Here, $\mathbf{k} = k_{\perp} \hat{x} + k_{\parallel} \hat{z}$ is the wave vector, ω is the complex frequency, c is the speed of light, \mathbf{I} is the unit dyadic, and $\boldsymbol{\sigma}$ is the conductivity tensor.

Regardless of the algorithm used, we may have to limit the computation space by preliminary analytic estimates as to which modes are the most likely to be unstable, and by using thermodynamic estimates of the amount of free energy in the distribution functions to direct our computational attention to specific, limited regions of the plume.

F. Nonlinear Wave Amplitude Limits within the Plume

Since the VF-200TM firings will be long compared to most wave mode growth times, the non-linear excitation limit of the amplitude of the dominant wave modes and the damping mechanisms of those modes in other regions of the plume are of interest. To this end, we will attempt to corroborate results of the dispersion analysis and of the macroscopic stability analysis with experimental measurements of the vector electric field, magnetic field, and plasma density fluctuations; i.e. if the models indicate a large growth rate in a particular region of configuration and frequency space, we should expect to measure a significant wave amplitude. Ideally, we could use the probe measurements as an exclusive determination of the wave amplitudes inside the plume. However, there are regions of the plume that are inaccessible to probes (see Figure 2). Additionally, we desire to model a nonlinear limit of the dominant wave amplitudes consistently with our equilibrium plasma parameters. Comparison of modeled amplitudes with measured amplitudes will be important for checking the accuracy of our instability models.

The most general way to numerically simulate the nonlinear dynamics of plasma waves is to use an electromagnetic particle-in-cell simulation. The particle positions and velocities are advanced in time by Newton's Second Law, while the fields and charge quantities are stored on a grid and advanced using finite differencing of Maxwell's equations. Particle codes are computer resource intensive and are typically tailored to a specific problem so that only relevant physical space and time scales are resolved.

G. Wave Propagation through the Plasma and Emission at the Plasma-Vacuum Interface

To model wave propagation through the plume we will use either a ray tracing algorithm or a full wave simulation. The choice will depend on the particular mode being investigated and its expected behavior at the edge of the plume. Ray tracing methods have the advantage of being computationally less intense, although they do not treat mode conversion as naturally as full-wave codes. To model the linear growth or damping of the wave, the ray tracing calculations must use complex wave numbers or be coupled with Fokker Planck codes to model the interaction with the plasma distribution function. The latter technique is well documented as a method to model radio frequency heating in fusion energy application.¹³ Since we presume to have measured the distribution functions that coexist with an identified wave mode, our ray tracing calculations must take place in complex space so that the growth or damping of the wave can be modeled consistently.

One possible ray-tracing technique is R. Horne's HOTRAY code, which models wave propagation and growth in a hot, anisotropic plasma.¹⁴ This code was developed to study the generation of radiation in the terrestrial magnetosphere. The algorithm uses the geometric optics method, and therefore assumes that plasma parameters do not change significantly along one wavelength. HOTRAY determines the ray path by integrating Hamilton's equations (Eqs. (1) and (2)) with the condition that the hot plasma dispersion relation must be satisfied.

$$\frac{d\mathbf{x}}{dt} = - \frac{\partial D}{\partial \mathbf{k}} / \frac{\partial D}{\partial \omega} \quad (2)$$

$$\frac{d\mathbf{k}}{dt} = \frac{\partial D}{\partial \mathbf{x}} / \frac{\partial D}{\partial \omega} \quad (3)$$

$$D(\mathbf{x}, \mathbf{k}, \omega) = 0 \quad (4)$$

$$\Gamma = \sum k_i \cdot \Delta x \quad (5)$$

Here, \mathbf{x} is the position vector of a point along the ray path, ω is the angular wave frequency, \mathbf{k} is the wave vector, D is the dispersion relation, and Γ is the path-integrated growth rate. The algorithm uses real ω and \mathbf{k} to integrate Eqs. (2) and (3), but the complex wave number ($k + k_i$) is found from solving the dispersion relation at each new point in space. The growth rate can then be calculated by Eq. (5). The imaginary part of \mathbf{k} , is assumed to be small compared to the real part, so the method is only valid for weakly damped or growing waves.

For regions of physical or frequency space for which the ray-tracing assumptions are not valid, the next choice of simulation technique is full-wave modeling. Full-wave algorithms solve for the fields throughout the entire plasma at each time step, and some algorithms can model arbitrarily high harmonics of the cyclotron frequency¹⁵. Additionally, with sufficient resolution, full wave simulations can accurately model wave mode conversion processes. At the vacuum interface, an electrostatic mode will need to couple to an electromagnetic mode in order for the wave energy to leave the plasma (for example, see ¹⁶).

The limits of full-wave algorithm are encountered when the assumptions that $kp \ll 1$ or $\rho/L \ll 1$ become invalid. Here, ρ is the gyroradius and k is the wave number. AORSA is one code that eliminates the concern about kp , because it does not make an expansion involving this quantity. The ρ/L assumption must still be satisfied however, which can become problematic for frequencies near f_{ci} in regions where the ion gyroradius is becoming large compared to spatial scale lengths.

H. PIC as an Alternative

In principle, particle-in-cell simulation could be used as a substitute for any of the numerical procedures listed above. Given sufficient resolution, particle codes can model instability growth, nonlinear wave interactions and wave propagation. However, because they require so much computer time and self-consistent initialization of distribution functions, we will use particle simulations only if justified by experimental observation. Particle simulations might be used to evaluate approximations for selected instabilities or to benchmark the less explicit methods of our instability analysis.

I. Receiving Antenna Measurements

We will measure the vacuum radiated fields in the downstream section of the vacuum chamber. The receiving antenna will be placed in a region outside of the plasma plume, and measurements will be made to as many specifications of MIL-STD-461 as practical.

The steel walls of the vacuum chamber will also act as a reverberating chamber where the EMI will excite distinct chamber modes which may obscure the actual EMI emissions. To prevent from obscuring radiated emissions levels, MIL-STD-461 requires that radio frequency absorbers be installed on all walls surrounding the equipment under test. Such an installation in our vacuum chamber would be very expensive and time consuming. The absorbing material would likely not be suited to long term operation in a plasma discharge, and would therefore need to be removed after EMI testing was complete.

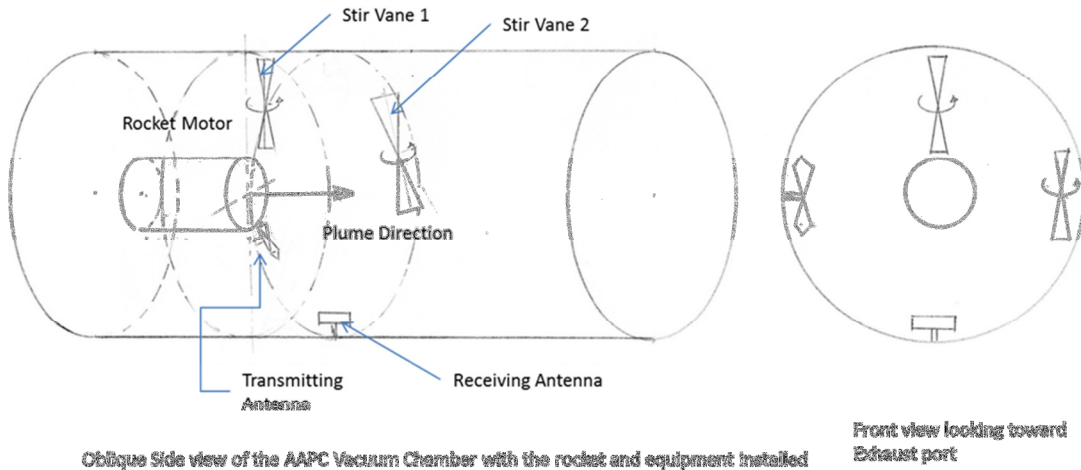


Figure 7. Chamber Set Up as a Reverberation Chamber with Mode Stirrers, a Possible Alternative to Using RF Absorbing Material

A possible alternative to the use of RF absorbers is mode-stirring. Methods for measuring EMI in a reverberating chamber have been theorized for rectangular chambers.^{17,18} The methods use multimode resonance mixing whereby mode stirring devices continuously vary the geometry inside the chamber so that resonant modes close to each other are smoothly coupled. Mechanical mixing vanes were first suggested as the means for mixing.¹⁸ However, more recently electronic mode stirring has been developed.¹⁹ Mechanical mode mixing has been shown to produce a uniform field in the test chamber away from the chamber walls, test article and other boundaries.²⁰ Figure 7 shows a possible arrangement of mode stirrers in the AARC chamber.

A possible reverberating chamber testing procedure could be as follows.¹⁸ First, the test article is activated and run through a test cycle. Next, a calibrated signal generator attached to an antenna with known characteristics is used. The signal is adjusted until it matches the signal received during testing. The signal from the calibrated antenna is then related to the signal measured from the test article. Recommendations for the use of a reverberating chamber are published in MIL-STD-461 (latest revision), although the standard allows the use of reverberating chambers only for testing of susceptibility, not for emissions. The reverberation chamber method is also limited to a minimum frequency, based on the size of the chamber. This low frequency limit is based on requiring a certain density of modes in the chamber.³

J. Extending the Study to the VF-200™

The testing described above will involve the VX-200 prototype, which is a single-core thruster. The VF-200™ flight model, on the other hand, will utilize a quadrupole magnet configuration with side-by-side thrusters. The VF-200™ plume may potentially produce EMI that is not present in the dipole configuration of the VX-200 prototypes. Modeling the oppositely polarized side-by-side thrusters will be addressed in a subsequent study. Estimates of EMI from the plasma plume will eventually be compared to on-orbit measurements from the Aurora Plasma Diagnostics Platform (APDP), which will contain a suite of diagnostic probes designed to study a wide variety of physics in the VF-200™ plume.²¹ To predict the on-orbit emissions, we will attempt to modify the boundary conditions of any successful simulations. For instance, the boundary of the full-wave model could be altered so that the outgoing waves are perfectly absorbed.

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